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Panel Data with Errors-in-Variables: A Note on Essential and Redundant Orthogonality Conditions in GMM-estimation

$$+ \frac{1}{2} \sum_{i>j} \sum_{j=1} \text{cov}_a(X_i, X_j)$$

$$\text{var}\left(\sum_{i=1}^n a_i X_i\right) = \sum_{s=0}^{t-1} a_s \text{var}\left(\sum_{k=s+1}^{t-1} a_k\right) b_s$$

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Abstract:

General Method of Moments (GMM) estimation of a linear one-equation model using panel data with errors-in-variables is considered. To eliminate fixed individual heterogeneity, the equation is differenced across one or more than one periods and estimated by means of instrumental variables. With non-autocorrelated measurement error, we show that only the one-period and a few two-period differences are essential, i.e. relevant for GMM-estimation. GMM estimation based on all orthogonality conditions on the basis of a generalized inverse formulation is shown to be equivalent to estimation using only the essential orthogonality conditions

Keywords: Panel Data, Errors-in-Variables, Instrumental Variables, GMM Estimation, Generalized inverse

JEL classification: C23, C33, C12, C13.

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1 Introduction

Estimation and testing of econometric models for panel data by means of the Generalized Method of Moments (GMM) has received considerable attention in recent years; see Baltagi (1995, especially ch. 8) for a survey. GMM estimation can be used for consistent and asymptotically efficient estimation of linear equations with endogenous right-hand side variables, with lagged values of left-hand side variables as right-hand side variables, with random measurement errors in the right-hand side variables, and for some kinds of nonlinear models.

The focus in this paper is on the errors-in-variables problem for panel data in a single linear static equation context, although several of the procedures and the results below may also be made applicable to other, more complex, situations. A primary motivation of the paper is to elaborate the *matrix algebra for GMM estimation of differenced equations and the associated orthogonality conditions* in a panel data context in more detail than is commonly given in the literature, cf. e.g. Griliches and Hausman (1986). We specifically discuss a rank problem which arise when using GMM estimation of equations expressed as differences in an errors-in-variables context, when the various differenced equations and the associated orthogonality conditions are not linearly independent. This rank problem can be handled by either (i) replacing the standard inverses in the expressions for the GMM estimators by *generalized (Moore-Penrose) inverses*, or (ii) eliminating the redundant orthogonality conditions from the GMM procedure, as we prove to be equivalent and computationally more attractive.

2 Instrumental variable estimation for panel data with errors-in-variables.

2.1 The basic model

Consider a balanced set of panel data for N units or groups in T successive periods and the relationship between a left-hand side variable y and a right-hand side variable x (both scalars). The analysis is limited to the case with only one regressor for convenience, as did Griliches and Hausman (1986), but the insights can be generalized rather straightforwardly to cases with several regressors. Let y_{it} and x_{it} denote their values for observation unit i (in the following denoted as individual i) in period t , satisfying

$$y_{it} = x_{it} \beta + a_i + u_{it}, \quad i = 1, \dots, N; t = 1, \dots, T, \quad (1)$$

where a_i is a fixed effect (including a common constant term), specific to individual i , β is an unknown scalar constant, and u_{it} is a zero mean, random disturbance/error term. We assume,

owing to endogeneity of x_{it} or random measurement error in x_{it} , (i) that u_{it} is correlated with x_{it} , (ii) that u_{it} is uncorrelated with u_{js} for all $j \neq i$, and (iii) that u_{it} is uncorrelated with x_{is} for all i and some $s \neq t$. We will mostly focus on the case where u_{it} is uncorrelated with u_{is} for all $t \neq s$, but we will discuss more general cases in section 3.3. It is convenient to rewrite (1) as N vector equations, one for each individual i :

$$\underline{y}_i = \underline{x}_i \beta + a_i \otimes e_T' + \underline{u}_i, \quad i = 1, \dots, N. \quad (2)$$

where \underline{y}_i , \underline{x}_i and \underline{u}_i are $(1 \times T)$ vectors (with y_{it} , x_{it} and u_{it} from individual i as elements), \otimes is the Kronecker product operator, $a = (a_1 \dots a_N)$ and $e_T = (1 \dots 1)'$ is a $(T \times 1)$ vector of ones.

In order to eliminate a_i from (2), we will work with observations differenced across time periods. If $T > 2$, these differences can be taken across $1, 2, \dots, T - 1$ periods. To formalize this, we introduce the *differencing vectors*

$$D_{ts} = \left[\begin{array}{c} (1 \times T) \text{ vector with} \\ \text{element } t = +1, \text{ element } s = -1, \\ \text{and zero otherwise} \end{array} \right], \quad t, s = 1, \dots, T; t > s, \quad (3)$$

where $t > s$ can be assumed without loss of generality. Premultiplying a $(T \times 1)$ vector by D_{ts} takes a difference between its t 'th and s 'th elements. Since there are $S = \frac{1}{2}T(T-1)$ different ways of drawing two elements from T , there are S such D_{ts} vectors, among which $T-1$ take differences across one period, $T-2$ across two periods, \dots , two across $T-2$ periods, and one across $T-1$ periods. The differencing vectors are not independent, since all $S - (T-1) = \frac{1}{2}(T-1)(T-2)$ differences over two or more periods can be constructed from the $T-1$ one-period differences, formally $D_{ts} = \sum_{j=s+1}^t D_{j,j-1}$, with $t > s$ and $t, s = 1, \dots, T$. Postmultiplying through (2) by D'_{ts} , recalling that $D_{ts}e_T = 0$, we get $\underline{y}_i D'_{ts} = \underline{x}_i D'_{ts} \beta + \underline{u}_i D'_{ts}$, or

$$y_{it} - y_{is} = (x_{it} - x_{is})\beta + (u_{it} - u_{is}), \quad t, s = 1, \dots, T; t > s, \quad (4)$$

Defining the stacked $(S \times T)$ differencing matrix

$$D = \left[D'_{21} \ D'_{32} \ \dots \ D'_{T,T-1} \ D'_{31} \ D'_{42} \ \dots \ D'_{T,T-2} \ \dots \ D'_{T1} \right]', \quad (5)$$

we can rewrite (4) as:

$$Y_i = X_i \beta + U_i, \quad i = 1, \dots, N, \quad (6)$$

where

$$\begin{cases} Y_i = D \underline{y}'_i, \\ X_i = D \underline{x}'_i, \\ U_i = D \underline{u}'_i, \end{cases} \quad i = 1, \dots, N.$$

(6) may be considered a system of S equations with a common slope coefficient β and with N observations of each equation. When different pairs of periods are involved, we always assume that the pairs of periods (t, s) are ordered in the same way as in (5).

2.2 Instrumental variables and the orthogonality conditions

The structural parameter β in the model can be estimated using lagged and leaded x 's as instrumental variables if the measurement errors in the x 's are non-autocorrelated, as was shown by Griliches and Hausman (1986). Specifically, if we consider (4) for two given periods t and s , valid instruments are $x_{i\tau}$ for $\tau \neq t, s$ ($\tau = 1, \dots, T$)¹. Consequently, we have different instruments for each of the S equations in (6), and consequently a GMM-procedure is called for to estimate β from the whole system of equations jointly.

The idea we follow is, for one pair of periods (t, s) , to use as IV's all the $T - 2$ elements of \underline{x}_i for the $T - 2$ periods which are not used in the construction of the differenced variables in (4). A similar general idea has been followed in the literature on dynamic panel data models², and by Griliches and Hausman (1986), for panel data models with errors in variables³. We define the $S = \frac{1}{2}T(T - 1)$ selection matrices

$$P_{ts} = \begin{bmatrix} ((T - 2) \times T) \text{ matrix} \\ \text{obtained by deleting} \\ \text{rows } s \text{ and } t \text{ from } I_T \end{bmatrix}, \quad t, s = 1, \dots, T; \quad t > s, \quad (7)$$

and

$$z_{its} = \underline{x}_i P'_{ts} = \begin{bmatrix} (1 \times (T - 2)) \text{ vector} \\ \text{obtained by deleting} \\ \text{elements } s \text{ and } t \text{ from } \underline{x}_i \end{bmatrix}, \quad \begin{array}{l} i = 1, \dots, N; \\ t, s = 1, \dots, T; \\ t > s. \end{array} \quad (8)$$

To carry out GMM estimation of β based on the complete system of S equations, we must stack the instruments as follows. Define the $(S \times S(T - 2))$ IV matrix for individual i

$$Z_i = \begin{bmatrix} z_{i21} & 0 & \cdots & 0 \\ 0 & z_{i32} & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & z_{iT1} \end{bmatrix} = \begin{bmatrix} \underline{x}_i P'_{21} & 0 & \cdots & 0 \\ 0 & \underline{x}_i P'_{32} & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & \underline{x}_i P'_{T1} \end{bmatrix},$$

which can be written as

$$Z_i = (I_S \otimes \underline{x}_i) P', \quad (9)$$

¹This requires, of course, that $\text{plim}_{N \rightarrow \infty} [(1/N) \sum_{i=1}^N x_{i\tau}(x_{it} - x_{is})] \neq 0$ in addition to $\text{plim}_{N \rightarrow \infty} [(1/N) \sum_{i=1}^N x_{i\tau}(u_{it} - u_{is})] \neq 0$.

²See Baltagi (1995, chapter 8) for a survey.

³See also Biørn (1996, section 10.2.3).

where P is the $(S(T-2) \times ST)$ matrix, containing only zeros and ones,

$$P = \begin{bmatrix} P_{21} & 0 & \cdots & 0 \\ 0 & P_{32} & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & P_{T1} \end{bmatrix}. \quad (10)$$

Premultiplying (6) by Z_i' , we get

$$Z_i' Y_i = Z_i' X_i \beta + Z_i' U_i, \quad i = 1, \dots, N. \quad (11)$$

The orthogonality conditions which are *a priori* relevant to GMM estimation of β based on (11) can be stated:

$$\mathcal{E}(Z_i' U_i) = \underline{0}, \quad i = 1, \dots, N. \quad (12)$$

where $\underline{0}$ is a $(S(T-2) \times 1)$ vector of zeros, i.e. (12) represents $S(T-2)$ scalar orthogonality conditions.

2.3 The GMM-estimator and the generalized inverse

Some of the elements in the (vector) equation (12) are redundant, as they do not contain additional information. This can be seen by noticing that for say $l < s$ (or $l > t$) we have that

$$\mathcal{E}[x_{il}(u_{it} - u_{is})] = \mathcal{E}[x_{il}(u_{i,s+1} - u_{is})] + \cdots + \mathcal{E}[x_{il}(u_{it} - u_{i,t-1})]. \quad (13)$$

That is, the orthogonality condition $\mathcal{E}[x_{il}(u_{it} - u_{is})] = 0$ can be constructed as a simple sum of the orthogonality conditions on the right hand side of (13). As a consequence, the variance-covariance matrix needed for GMM estimation on the basis of (11) and (12) does not have full rank. We will elaborate on this point below.

Denote the (reduced rank) variance-covariance matrix associated with (12) by Ω_i , i.e.

$$\Omega_i = \mathcal{E}(Z_i' U_i U_i' Z_i). \quad (14)$$

White (1986) has considered efficient estimation based on orthogonality conditions such as (12), in the general case where Ω_i might not have full rank. Using Theorem 3.2 in White, we find that the asymptotically efficient GMM estimator $\hat{\beta}$, based on the orthogonality conditions (12) for $i = 1, \dots, N$, can be written:

$$\hat{\beta} = \left[\left(\sum_i X_i' Z_i \right) \left(\sum_i \Omega_i \right)^+ \left(\sum_i Z_i' X_i \right) \right]^{-1} \left(\sum_i X_i' Z_i \right) \left(\sum_i \Omega_i \right)^+ \left(\sum_i Z_i' Y_i \right), \quad (15)$$

where the sums cover all individuals and $(\sum_i \Omega_i)^+$ is the generalized inverse of $\sum_i \Omega_i$.

3 Identification of essential orthogonality conditions

3.1 The essential orthogonality conditions

Even though the estimator (15) is efficient in a statistical sense, it is not very efficient in a computational sense. Computationally it is more efficient to consider only the *essential* orthogonality conditions, which we will now identify. In the case with non-autocorrelated errors u_{it} , we show formally below that all orthogonality conditions can be constructed as simple sums of (i) all admissible orthogonality conditions based on one-period differences and (ii) a specific subset of the admissible orthogonality conditions based on two-period differences. All the other orthogonality conditions can be ignored.

The orthogonality conditions (12) are based on expressions of the form $\mathcal{E}[x_{il}(u_{it} - u_{is})] = 0$ where $l \neq t, s$. However, all these orthogonality conditions can be constructed as simple sums of

- (i) $\mathcal{E}[x_{il}(u_{it} - u_{i,t-1})] = 0, l \neq t, t - 1,$
- (ii) $\mathcal{E}[x_{il}(u_{i,l+1} - u_{i,l-1})] = 0.$

This is easily seen as follows: First, when $l \notin [s, s + 1, \dots, t - 1, t]$, any orthogonality condition $\mathcal{E}[x_{il}(u_{it} - u_{is})] = 0$ can be constructed on the basis of expressions as in (i), using the identity

$$\mathcal{E}[x_{il}(u_{it} - u_{is})] = \sum_{\tau=s+1}^t \mathcal{E}[x_{il}(u_{i\tau} - u_{i,\tau-1})].$$

Second, when $l \in [s + 1, s + 2, \dots, t - 2, t - 1]$, expressions both of the forms (i) and (ii) must be combined, using

$$\mathcal{E}[x_{il}(u_{it} - u_{is})] = \sum_{\tau=l+2}^t \mathcal{E}[x_{il}(u_{i\tau} - u_{i,\tau-1})] + \mathcal{E}[x_{il}(u_{i,l+1} - u_{i,l-1})] + \sum_{\tau=s+1}^{l-1} \mathcal{E}[x_{il}(u_{i\tau} - u_{i,\tau-1})],$$

since $\mathcal{E}[x_{il}(u_{il} - u_{i,l-1})] = 0$ and $\mathcal{E}[x_{il}(u_{i,l+1} - u_{il})] = 0$ are inadmissible whereas $\mathcal{E}[x_{il}(u_{i,l+1} - u_{i,l-1})] = 0$ is admissible. Hence, any orthogonality condition of the form $\mathcal{E}[x_{il}(u_{it} - u_{is})] = 0$ where $l \neq (t, s)$, can be constructed from the two kinds of orthogonality conditions (i) and (ii).

It follows that the number of essential orthogonality conditions is⁴ $T(T - 2)$, while the total number of orthogonality conditions is $T(T - 1)(T - 2)/2$. Hence, only a fraction $2/(T - 1)$ of the complete set of orthogonality conditions are essential. E.g., for $T = 9$, this fraction is one fourth.

We have shown that only orthogonality conditions based on the one-period and a few two-period differences are essential. We refer to the other orthogonality conditions as redundant. With autocorrelated noise, higher order differences replace the two-period differences; see Biørn and Klette (1997).

⁴Among these, $(T - 1)(T - 2)$ are based on one-period differences, and $(T - 2)$ on two-period differences.

3.2 The equivalence of the two GMM-estimators

It follows from section 3.1 that there exists a matrix H of zeros and ones such that

$$[Z'_i U_i]_R = H [Z'_i U_i]_E, \quad (16)$$

where subscripts R and E denote the elements associated with the sets of redundant and essential orthogonality conditions respectively. More generally, we have

$$\begin{bmatrix} (Z'_i Y)_R & (Z'_i X_i)_R & (Z'_i U_i)_R \end{bmatrix} = H \begin{bmatrix} (Z'_i Y)_E & (Z'_i X_i)_E & (Z'_i U_i)_E \end{bmatrix}. \quad (17)$$

Define

$$K = \begin{bmatrix} I_{T(T-2)} \\ H \end{bmatrix},$$

where $I_{T(T-2)}$ is the identity matrix of order $T(T-2)$. Stacking $Z'_i U_i$ as follows

$$Z'_i U_i = \begin{bmatrix} (Z'_i U_i)_E \\ (Z'_i U_i)_R \end{bmatrix},$$

and using (16), we have

$$\begin{aligned} \Omega_i &= \mathcal{E} [Z'_i U_i U'_i Z_i] \\ &= K \mathcal{E} [(Z'_i U_i)_E (U'_i Z_i)_E] K' \\ &= K \Omega_{E,i} K' \end{aligned} \quad (18)$$

where $\Omega_{E,i}$ is defined by the last equality. Using (17) and (18), the GMM estimator in (15) can be rewritten

$$\begin{aligned} \hat{\beta} &= \left\{ \left(\sum_i X'_i Z_i \right)_E K' \left[K \left(\sum_i \Omega_{E,i} \right) K' \right]^+ K \left(\sum_i Z'_i X_i \right)_E \right\}^{-1} \times \\ &\quad \left(\sum_i X'_i Z_i \right)_E K' \left[K \left(\sum_i \Omega_{E,i} \right) K' \right]^+ K \left(\sum_i Z'_i Y_i \right)_E. \end{aligned} \quad (19)$$

The definition of the generalized inverse implies

$$(K \Omega_E K') (K \Omega_E K')^+ (K \Omega_E K') = (K \Omega_E K'),$$

where we have used Ω_E as a short-hand notation for $\sum_i \Omega_{E,i}$. Pre- and postmultiplying this equation by $\Omega_E^{-1} (K' K)^{-1} K'$ and $K (K' K)^{-1} \Omega_E^{-1}$ respectively, we find that

$$K' (K \Omega_E K')^+ K = \Omega_E^{-1}. \quad (20)$$

Inserting (20) into (19), we find that

$$\hat{\beta} = \left[\left(\sum_i X'_i Z_i \right)_E \left(\sum_i \Omega_{E,i} \right)^{-1} \left(\sum_i Z'_i X_i \right)_E \right]^{-1} \left(\sum_i X'_i Z_i \right)_E \left(\sum_i \Omega_{E,i} \right)^{-1} \left(\sum_i Z'_i Y_i \right)_E$$

Hence, the GMM-estimator based on the complete set of orthogonality conditions is *equivalent* to the GMM-estimator based on only the essential orthogonality conditions.

As remarked above, the essential set of orthogonality conditions constitutes a fraction $2/(T - 1)$ of the complete set of orthogonality conditions. Exploiting only the former can reduce the computational burden considerably, in particular related to inverting the variance-covariance matrix $(\sum_i \Omega_i)$. With a moderately long panel such as $T = 9$, using the complete set of orthogonality conditions, this matrix has dimension (252×252) , which is reduced to (63×63) when using only the essential orthogonality conditions.

Here we should point out that with more than one regressor, say G regressors, the dimensionality of the IV matrix Z_i and hence the variance-covariance matrix Ω_i will grow in proportion to G , while the fraction $2/(T - 1)$ of the complete set of orthogonality conditions that is essential remains the same. Hence, with $G = 3$ and $T = 9$, Ω_i will have dimension (756×756) , while $\Omega_{E,i}$ has dimension (189×189) . Whether it is a good idea in practice to use all essential orthogonality conditions (as defined above) with $T = 9$ and $G = 3$ depends on the sample size and the stochastic processes for the regressors. However, these are issues discussed elsewhere under the labels “overfitting” and “weak instruments”; see e.g. Davidson and MacKinnon (1993, chs. 7 and 17) and Staiger and Stock (1994, 1996).

In Biørn and Klette (1997) we elaborate on the analysis above and show, in particular, how to identify the essential orthogonality conditions in cases with autocorrelated measurement errors.

4 Final remarks

This note has examined the orthogonality conditions relevant for GMM estimation of differenced equations from panel data with errors-in-variables, using variables in levels as IVs for differenced variables. We have shown that with non-autocorrelated measurement errors, only a small fraction of the potential orthogonality conditions are essential, namely those based on one-period and a few two-period differences. When only predetermined variables are valid instruments as in *autoregressive* panel data models, even the two-period differences are inadmissible, and one is left only with the orthogonality conditions based on one-period differences.

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